

**GUJARAT TECHNOLOGICAL UNIVERSITY****BE - SEMESTER-VII (OLD) - EXAMINATION – SUMMER 2017****Subject Code: 171003****Date: 04/05/2017****Subject Name: Digital Signal Processing****Time: 02:30 PM to 05:00 PM****Total Marks: 70****Instructions:**

1. Attempt all questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.

**Q.1 (a)** Perform the linear convolution of the following two sequences: **07**  
 $x(n) = \delta(n) + \delta(n-1) + \delta(n-2)$   
 $h(n) = \delta(n-1) + \delta(n-2)$

**(b)** Sketch each of the following special digital sequences: **07**  
 (i)  $5\delta(n)$   
 (ii)  $-2\delta(n-5)$   
 (iii)  $-5u(n)$   
 (iv)  $5u(n-2)$

**Q.2 (a)** Derive the expression of recovering continuous time signal from discrete time samples. **07**

**(b)** Define the following types of discrete time systems: **07**  
 (i) Linear (ii) Time invariant (iii) stable (iv) Causal

**OR**

**(b)** Solve the linear difference equation given below: **07**  
 $y(n) - 0.5y(n-1) + 0.06y(n-2) = 2(0.1)^n$   
 $y(-1) = 1$  and  $y(-2) = 0$

**Q.3 (a)** Find the z-transform for each of the following sequences: **07**  
 (i)  $x(n) = 4u(n)$   
 (ii)  $x(n) = (-0.7)^n u(n)$   
 (iii)  $x(n) = 4e^{-2n} u(n)$

**(b)** Prove the following properties of z-transform: **07**  
 (i) Time shift (ii) Convolution

**OR**

**Q.3 (a)** Find  $y(n)$  if **07**  
 $Y(z) = (z^2(z+1)) / ((z-1)(z^2-z+0.5))$

**(b)** Find the inverse z-transform for each of the following functions: **07**

(i)  $X(z) = 2 + (4z / (z-1)) - (z / (z-0.5))$

(ii)  $X(z) = (5z / (z-1)^2) - (2z / (z-0.5)^2)$

**Q.4 (a)** Discuss the properties of Discrete Fourier Transform. **07**

**(b)** Explain the different structures for implementing discrete time systems. **07**

**OR**

**Q.4 (a)** Compare FIR filter with IIR filter. **07**

**(b)** Evaluate the DFT of  $x(n) = \delta(n) + 2\delta(n-1) + 3\delta(n-2) + 4\delta(n-3)$  **07**

**Q.5 (a)** Calculate the filter coefficients for a 5-tap FIR bandpass filter with a lower cutoff frequency of 2,000 Hz and an upper cutoff frequency of 2,400 Hz at a sampling rate of 8,000 Hz. **07**

**(b)** Given an analog filter whose transfer function is **07**  
 $H(s) = 10 / (s+10)$   
 Convert it to the digital filter transfer function and difference Equation, respectively, when a sampling period is given as T

=0.01 second. Use Bilinear Transformation method.

**OR**

- Q.5**   (a) Explain Goertzel algorithm. **07**  
          (b) Discuss the applications of Digital Signal Processing. **07**

\*\*\*\*\*