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**GUJARAT TECHNOLOGICAL UNIVERSITY BE - SEMESTER-III (NEW) - EXAMINATION - SUMMER 2017** Date: 25/05/2017 **Subject Code: 2130002 Subject Name: Advanced Engineering Mathematics** Time: 10:30 AM to 01:30 PM **Total Marks: 70 Instructions:** 1. Attempt all questions. 2. Make suitable assumptions wherever necessary. 3. Figures to the right indicate full marks. MARKS Q.1 **Short Questions** 14 What are the order and the degree of the differential 1 equation  $y''+3y^2 = 3\cos x$ . What is the integrating factor of the linear differential 2 equation:  $y' - (1/x) y = x^2$ 3 Is the differential equation  $ye^{x}dx + (2y + e^{x})dy = 0$  is exact? Justify. 4 Solve: y'' + 11 y' + 10 y = 0. 5 Find particular integral of :  $y'' + y' = e^{2x}$ 6 If  $y = (c_1 + c_2 x)e^x$  is a complementary function of a second order differential equation, find the Wronskian  $W(y_1, y_2).$ 7 Find the value of  $\Gamma\left(\frac{7}{2}\right)$ What is the value of the Fourier coefficients  $a_0$  and  $b_n$  for 8  $f(x) = x^2, -1 < x < 1.$ Find  $L\{e^{3t+3}\}$ 9 10 Find  $L^{-1}\left(\frac{4}{s^2} - \frac{1}{(s^2 + 9)}\right)$ Find the singular point of the differential equation 11  $(1 - x^{2})y'' - 2xy' + n(n + 1)y = 0$ 12 Obtain the general integral of  $\frac{\partial^3 z}{\partial z^3} = 0$ 13 Obtain the general integral of p + q = zState the relationship between beta and gamma function. 14 Q.2 03 (a) Solve:  $(x^2 + y^2 + 3)dx - 2xydy = 0$ (b) Solve:  $\frac{dy}{dx}$  + (tan x) y = sin 2x, y(0) = 0 04 (c)  $(D^4 - 16)y = e^{2x} + x^4$ , where  $D \equiv d / dx$ 07 (c) Use the method of variation of parameters to find the 07

general solution of  $y''-4y'+4y = \frac{e^{2x}}{x}$ 

Q.3 (a) Find half range sine series of 
$$f(x) = x^3$$
,  $0 \le x \le \pi$   
(b) Find the Fourier integral representation of the function  
 $f(x) = \begin{cases} 2, |x| < 2 \\ 0, |x| > 2 \end{cases}$   
(c) Find the Fourier series expansion for the  $2\pi$  - periodic  
function  $f(x) = x - x^2$  in the interval  $-\pi \le x \le \pi$  and show  
that  $\frac{1}{t^2} - \frac{1}{2^2} + \frac{1}{3^2} - \frac{1}{4^2} + \dots = \frac{\pi^2}{12}$   
OR  
Q.3 (a) Discuss about ordinary point, singular point, regular  
singular point and irregular singular point, regular  
of the differential equation:  $x^3(x-1)y^{n+3}($ 

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 $u_{tt} = c^2 u_{xx}, \ 0 \le x \le L$  satisfying the conditions:  $u(0,t) = u(L,t) = 0, \ u_t(x,0) = 0, \ u(x,0) = \frac{\pi x}{L}, 0 \le x \le L$ 

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