Enrolment No._____

GUJARAT TECHNOLOGICAL UNIVERSITY BE - SEMESTER-VII(NEW) • EXAMINATION – WINTER 2016

Subject Code:2171003 Subject Name:Digital Signal Processing Time:10.30 AM to 1.00 PM

Date:25/11/2016

Total Marks: 70

Instructions:

- 1. Attempt all questions.
- 2. Make suitable assumptions wherever necessary.
- 3. Figures to the right indicate full marks.
- Q.1 (a) State 'differentiation' and 'time convolution' properties for given transform 07 (Discrete Time Fourier Transform(DTFT) or Z-transform). Prove any one of two properties.
 - (b) List the classification of discrete time signals and also answer following : 07
 i) State whether following discrete time signal is periodic or not.

$$x(n) = \cos \frac{n}{6} \cos \frac{n\pi}{6}$$

ii) State whether following discrete time signal is energy signal or power signal or both or none of them.

$$x(n) = nu(n)$$

Q.2 (a) Using Z transform find i) impulse response and stability of the system 07 ii) step response described by following equation:

$$y(n) = 0.6y(n-1) + 0.08y(n-2) = x(n)$$

(b) Determine all possible signals that can have following z-transforms. 07

$$X(z) = \frac{1}{1 - 1.5Z^{-1} + 0.5Z^{-2}}$$

OR

- (b) Using properties of Z-transform ; find z-transform of following signals: i) x(n) = u(-n-2)ii) $x(n) = 2^n u(n-2)$
- Q.3 (a) State and derive necessary and sufficient condition for a discrete time system 07 to be BIBO stable.
 - (b) Obtain direct form II realization of the LTI system presented by equation: 07

$$y(n) = -\frac{13}{12}y(n-1) - \frac{9}{24}y(n-2) - \frac{1}{24}y(n-3) + x(n) + 4x(n-1) + 3x(n-2)$$

- Q.3 (a) Explain importance of transforms. Explain with necessary equations, relation 07 of i) z-transform to Discrete Time Fourier transform (DTFT) and ii) z-transform to Discrete Fourier transform (DFT) and compare them.
 - (b) Find the direct form -I realization of discrete time system represented by 07 transfer function:

$$H(Z) = \frac{2z^3 - 7z^2 + 6z - 1}{[z - (1/3)][z^2 - 2Z + (1/4)]}$$

- Q.4 (a) Enlist the various methods to design IIR filter from analog filters. List 07 desirable properties to convert analog filters into digital filters. Explain any one IIR filter design techniques in brief.
 - (b) Explain 8-point DFT from two 4 point DFTs using radix-2 Decimation in 07 frequency (DIF) FFT algorithm.

OR

Q.4 (a) Find out filter order N and cut off frequency Ω_c in order to design IIR butter 07 worth digital filter using bilinear transformation. Take T =1 s. The design specifications of desired low pass filter are :

$$0.85 \le |H(w)| \le 1; \dots \dots 0 \le \omega \le \frac{\pi}{2}$$
$$|H(w)| \le 0.15, \dots, \frac{3\pi}{4} \le \omega \le \pi$$

- (b) Explain 8-point DFT from two 4 point DFTs using radix-2 Decimation in 07 Time (DIT) FFT algorithm.
- Q.5 (a) Define terms i) multi-rate signal processing and ii) down sampling. Explain 07 concept of down sampling with the help of simple example. Explain aliasing effect and concept of anti-aliasing filter.
 - (b) A filter is to be designed with the following desired frequency response . 07

$$H_{d}(e^{jw}) = 0....for....\frac{-\pi}{2} \le \omega \le \frac{\pi}{2}$$
$$H_{d}(e^{jw}) = e^{-2jw}....for....\frac{\pi}{2} \le \omega \le \pi$$

Determine the filter coefficients h(n), if the window function is defined as $w(n)=1,\ldots,for,\ldots,0 \le n \le 4$

w(n) = 0....othwrwise

Also determine frequency response H(e^{jw}) of the desired filter.

OR

- Q.5 (a) Explain concept of forward/backward linear prediction with necessary 07 equations and any one of its application (block diagram only).
 - (b) Explain pipelining in context of microprocessors. Enlist pipeline phases in 07 different TMS320 processors.

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