

GUJARAT TECHNOLOGICAL UNIVERSITY
B. E. - SEMESTER – VII • EXAMINATION – WINTER 2012

Subject code: 171701**Date: 26/12/2012****Subject Name: Control System Design****Time: 10.30 am - 01.00 pm****Total Marks: 70****Instructions:**

1. Attempt any five questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.

Q.1 (a) What is compensation? What are the different types of compensation? **07**
 Explain lead compensation network in detail.

(b) Derive z- Transform of given continuous signals with sampling time:

(i) $\frac{s}{s^2 + \omega^2}$; $T_s = T$ **03**

(ii) $\frac{s+2}{s^2 + 5s + 6}$; $T_s = 1 \text{ sec}$ **04**

Q.2 (a) Define controllability and observability. Find both for second order system given by differential equation **07**

$$\ddot{y} + 2\dot{y} + y = \dot{u} + u$$

with $x_1 = y$, $x_2 = \dot{y} - u$.

(b) The open loop transfer function of dc motor is $\frac{K}{s(s+2)(s+4)}$. Design suitable compensator for damping ratio=0.5 and $\omega_n = 3 \text{ rad/sec}$. **07**

OR

(b) For an aircraft position control system having open loop transfer function is $\frac{K}{s(s+3)(s+6)}$. Design suitable compensator for $\omega_n = 2 \text{ rad/sec}$, damping ratio=0.5 and $K_v \geq 10 \text{ sec}^{-1}$. **07**

Q.3 (a) A system has a plant transfer function $G_p(s) = \frac{4}{s+2}$. (i) Determine $G(z)$ for $G_p(s)$ preceded a zero order hold with $T=0.1 \text{ sec}$. (ii) Determine whether the digital system is stable. (iii) Plot the step response of $G(z)$ for the first 5 samples. **07**

(b) Explain internal model design in detail for a step reference input. **07**

OR

Q.3 (a) Consider the system $G_p(s) = K/s^2$ with PD controller having transfer function $(1+10s)$. For given system preceded by a zero order hold with $T=1 \text{ sec}$. (i) determine Z transform (ii) plot root locus (iii) determine value K for stability. **07**

(b) Explain the compensator design with integrated full-state feedback and observer. **07**

Q.4 (a) Define robust control system with system sensitivity. Explain how to analysis the robustness of the system. **07**

(b) A magnetically suspended steel ball described by $A = \begin{bmatrix} 0 & 1 \\ 3 & 0 \end{bmatrix}$, $B = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$. Design state feedback controller such that system have damping ratio=1 and $t_s = 2 \text{ sec}$. **07**

OR

Q.4 (a) Explain the robust internal model control system. **07**

Q.4 (b) A second order system given by $A = \begin{bmatrix} 0 & 1 \\ 0 & -1 \end{bmatrix}$, $B = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$. Design optimal feedback controlled system using ricatti equation for $Q = \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix}$, $R = [1]$. **07**

Q.5 (a) A unity feedback control system has an open-loop transfer function of $G(s) = K/s^2$. Design a lead compensator such that $K_a = 1$ and $PM \geq 45^\circ$. **10**

(b) How to find out stability of system with uncertain parameters? **04**

OR

Q.5 The open loop transfer function of a robot position control system is $G(s) = \frac{3}{s(s+1)(0.5s+1)}$. Design a lag compensator such that $PM \geq 45^\circ$. **14**
