

**GUJARAT TECHNOLOGICAL UNIVERSITY**  
**B. E. - SEMESTER – VII • EXAMINATION – WINTER 2012**

Subject code: 171701

Date: 26/12/2012

Subject Name: Control System Design

Time: 10.30 am - 01.00 pm

Total Marks: 70

**Instructions:**

1. Attempt any five questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.

- Q.1** (a) What is compensation? What are the different types of compensation? Explain lead compensation network in detail. **07**
- (b) Derive z- Transform of given continuous signals with sampling time:
- (i)  $\frac{s}{s+\omega^2}$ ;  $T_s=T$  **03**
- (ii)  $\frac{s+2}{s^2+5s+6}$ ;  $T_s=1\text{sec}$  **04**

- Q.2** (a) Define controllability and observability. Find both for second order system given by differential equation **07**
- $$\ddot{y} + 2\dot{y} + y = \dot{u} + u$$
- with  $x_1=y$ ,  $x_2=\dot{y} - u$ .
- (b) The open loop transfer function of dc motor is  $\frac{K}{s(s+2)(s+4)}$ . Design suitable compensator for damping ratio=0.5 and  $\omega_n = 3$  rad/sec. **07**

**OR**

- (b) For an aircraft position control system having open loop transfer function is  $\frac{K}{s(s+3)(s+6)}$ . Design suitable compensator for  $\omega_n=2$  rad/sec, damping ratio=0.5 and  $K_v \geq 10 \text{ sec}^{-1}$ . **07**
- Q.3** (a) A system has a plant transfer function  $G_p(s) = \frac{4}{s+2}$ . (i) Determine  $G(z)$  for  $G_p(s)$  preceded a zero order hold with  $T=0.1$  sec. (ii) Determine whether the digital system is stable. (iii) Plot the step response of  $G(z)$  for the first 5 samples. **07**
- (b) Explain internal model design in detail for a step reference input. **07**

**OR**

- Q.3** (a) Consider the system  $G_p(s) = K/s^2$  with PD controller having transfer function  $(1+10s)$ . For given system preceded by a zero order hold with  $T=1\text{sec}$ . (i) determine Z transform (ii) plot root locus (iii) determine value K for stability. **07**
- (b) Explain the compensator design with integrated full-state feedback and observer. **07**

- Q.4** (a) Define robust control system with system sensitivity. Explain how to analysis the robustness of the system. **07**
- (b) A magnetically suspended steel ball described by  $A = \begin{bmatrix} 0 & 1 \\ 3 & 0 \end{bmatrix}$ ,  $B = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$ . Design state feedback controller such that system have damping ratio=1 and  $t_s=2\text{sec}$ . **07**

**OR**

**Q.4 (a)** Explain the robust internal model control system. **07**

**Q.4 (b)** A second order system given by  $A = \begin{bmatrix} 0 & 1 \\ 0 & -1 \end{bmatrix}$ ,  $B = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$ . Design optimal feedback controlled system using ricatti equation for  $Q = \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix}$ ,  $R = [1]$ . **07**

**Q.5 (a)** A unity feedback control system has an open-loop transfer function of  $G(s) = K/s^2$ . Design a lead compensator such that  $K_a = 1$  and  $PM \geq 45^\circ$ . **10**

**(b)** How to find out stability of system with uncertain parameters? **04**

**OR**

**Q.5** The open loop transfer function of a robot position control system is **14**

$G(s) = \frac{3}{s(s+1)(0.5s+1)}$ . Design a lag compensator such that  $PM \geq 45^\circ$ .

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