

**GUJARAT TECHNOLOGICAL UNIVERSITY**  
**BE - SEMESTER-VII • EXAMINATION – WINTER • 2014**

**Subject Code: 170103****Date: 04-12-2014****Subject Name: Mechanics of Composite Materials****Time: 10:30 am - 01:00 pm****Total Marks: 70****Instructions:**

1. Attempt all questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.

- Q.1 (a)** Derive longitudinal strength of a lamina. **07**
- (b)** Compute [A], [B], and [D] matrices for a [-60|0|+60] laminate. Material **07**  
 properties of the laminate are  $E_1=140$  GPa,  $E_2=10$  GPa,  $E_6=6$  GPa,  $\nu_{12} = 0.3$   
 and thickness = 0.2 mm. Define the type of laminate. Draw the sketch of the  
 laminate showing the height co-ordinates of top and bottom of each ply.

- Q.2 (a)** If the Reduced Stiffness Matrix of a material is given by: **07**

$$[Q] = \begin{bmatrix} 150.81 & 4.027 & 0 \\ 4.027 & 20.11 & 0 \\ 0 & 0 & 5 \end{bmatrix} \text{ GPa}$$

Determine  $E_1$ ,  $E_2$ ,  $G_{12}$  and  $\nu_{12}$  of the orthotropic lamina. How many planes of symmetry and independent elastic constant does an orthotropic material have?

- (b)** Explain strain-displacement relationship of a laminate. Draw relevant sketches. **07**
- OR**

- (b)** Write short note on: **07**
1. Differentiate between the structural behavior of isotropic materials and fibre reinforced composites.
  2. Sketch the variation of Young's modulus:  $E_x$  and  $E_y$  with  $\theta$  and explain the reason of variation.

- Q.3 (a)** Derive the laminate stiffness; [A], [B] and [D]. Start from inplane forces and **07**  
 moments of a laminate.

- (b)** Define on-axis and off-axis lamina. Describe the need of transformation in a fibre **07**  
 reinforced laminate. Explain what would happen if without performing  
 transformation stresses are calculated for a [90|0|90] laminate.
- OR**

- Q.3 (a)** Explain the stress and strain relations in a laminate and also explain and sketch **07**  
 the variation of stress and strain through a laminate.

- (b)** Describe in detail [A], [B] and [D] matrices, identify the couplings clearly. **07**

- Q.4 (a)** 1. A 45 degree lamina has stresses as mentioned below along the reference **07**  
 axes; determine the equivalent stress system of lamina along material  
 axes 1 and 2.  $\sigma_x = 200$  GPa,  $\sigma_y = 50$  GPa,  $\sigma_s = 70$  GPa

2. An isotropic lamina has  $E=100$  kN/m<sup>2</sup> and  $\nu=0.25$ . Determine the  
 reduced stiffness matrix and reduced compliance matrix.

- (b)** Explain the failure of unidirectional lamina under longitudinal tension. **07**
- OR**

- Q.4 (a)** 1. Determine the strain along the material axis 1-2 for a 30 degree lamina. **07**  
The strains along the reference axes are  $\varepsilon_x = 0.002$ ,  $\varepsilon_y = 0.0015$ ,  
 $\varepsilon_s = 0.00008$
2. Define stiffness and compliance matrices. **07**
- (b)** Explain Maximum Stress theory **07**
- Q.5 (a)** Write a short note on symmetric laminates **07**
- (b)** Compute the [A] matrix for a [-0|45|45|90]s. Thickness of each ply is 0.25 **07**  
mm.  $E_1=140\text{GPa}$ ,  $E_2=10\text{GPa}$ ,  $E_6=5\text{GPa}$  and  $\nu_{12} = 0.3$
- OR**
- Q.5 (a)** Write a short note on anti-symmetric laminates **07**
- (b)** Write a short note on the elastic properties of different kind of materials. Also **07**  
mention the number of independent elastic constants and planes of symmetry  
each of them have.

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