

GUJARAT TECHNOLOGICAL UNIVERSITY
MCA Sem – II Examination June 2011

Subject code: 620007

Subject Name : Theory of Computation

Date: 29/06/11

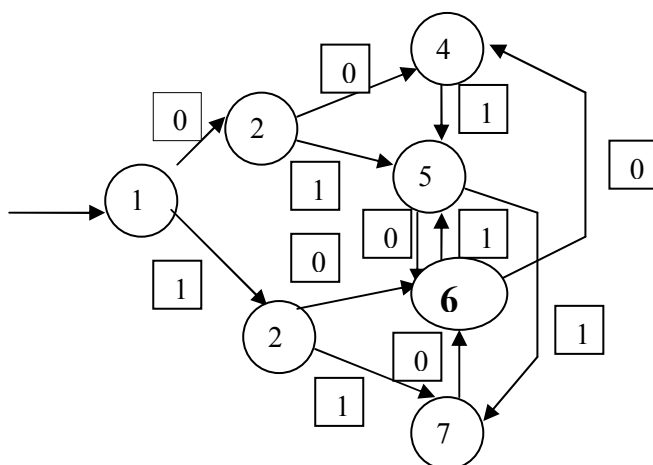
Total Marks: 70

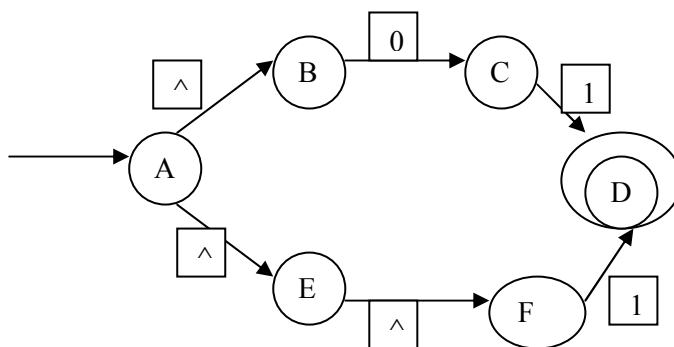
Time: 2:30pm to 5:00pm

Instructions:

1. Attempt all questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.

- Q.1 (a) What is Proposition? Which are logical connectives. 05
- (b) What is set ,Universal set and Complement set? List various set operators. 05
 Find regular expression for following languages over $\{0,1\}$. 04
- (c) (i) String end with 1.
 (ii) String of even length.
 (iii) String of size three or less than three.
 (iv) String containing substring 00.
- Q.2 (a) Give recursive definition for 04
 Set of all strings in $\{0,1\}^*$ containing substring 00 .
- (b) Prove that if either of a and b is even number the $a*b$ is even number. 03
- (c) Draw FA to recognize the following languages defined over $\{0,1\}^*$. 07
 (i) $(0+1)^*(110)$
 (ii) Language containing string of exactly two zeros.
- OR
- (c) Define FA and $\bar{\phi}^*$ for FA . 07
- Q.3 (a) Given that $L1 = \{x \in (0,1)^* \mid x \text{ ends with } 00\}$ 07
 $L2 = \{x \in (0,1)^* \mid x \text{ ends with } 10\}$
 Give FA for $L1$, $L2$ and $L1 \cup L2$.
- (b) Define NFA and $\bar{\phi}^*$ for NFA . 07
- OR
- Q.3 (a) Find minimal FA for following FA. **Note that state-6 is accepting state.** 07





- Q.4 (a) Let $M = (Q, \Sigma, q_0, \delta, A)$ where $Q = \{a, b, c, d\}$, $q_0 = a$ and $A = \{d\}$ and δ is given as follows. 07

State	input – 0	input -1
a	$\{b, d\}$	$\{c, d\}$
b	$\{b\}$	$\{d\}$
c	$\{d\}$	$\{c\}$
d	Φ	Φ

Give transition diagram for above NFA & find whether string 100101 will be accepted by it or not.

- (b) Explain and define Push Down Automata (PDA). 07

OR

- Q.4 (a) Find language corresponding to following CFG production. 07

- (i) $S \rightarrow aSa \mid bSb \mid \wedge$
 (ii) $S \rightarrow aS \mid bS \mid a$
 (iii) $S \rightarrow aSb \mid bSa \mid \wedge$
 (iv) $S \rightarrow aSa \mid bSb \mid a \mid b$

- (b) Draw Turing machine to accept $(a+b)^* aba (a+b)^*$. 07

- Q.5 (a) Write a short note on Derivation tree and ambiguity with reference to CFG. 05

- (b) Write a short note on recursive enumerable and recursive language. 05

- (c) Construct Turing machine to accept palindrome. 04

OR

- Q.5 (a) Explain Chomsky normal form with example. 05

- (b) Write short note on pumping lemma for CFL. 05

- (c) Draw NFA - \wedge corresponding to following regular expression over $\Sigma = \{0, 1\}$. 04

$(00+1)^*(10)^*$
