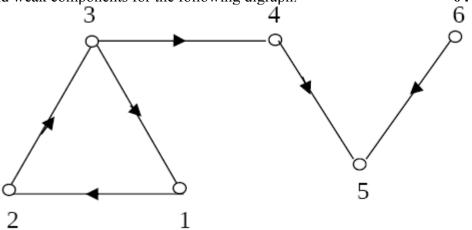
GUJARAT TECHNOLOGICAL UNIVERSITY MCA - SEMESTER-I • EXAMINATION – SUMMER 2013

WICA - SEMILSTER-I · EXAMINATION - SUMMER 2015							
Subject Code: 610003Date: 11-06-2013Subject Name: Discrete Mathematics for Computer ScienceTime: 10:30am to 13:00pmInstructions:							
 Attempt all questions. Make suitable assumptions wherever necessary. Figures to the right indicate full marks. 							
Q.1	(a)1.	Define Partial Order Relation and Poset. 2. Define Direct Product of lattices and Draw Hasse Diagrams of $\langle S, D \rangle$, $\langle L, D \rangle$ and $\langle S \times L, D \rangle$ for $S = \{1,3,6\}$ and $L = \{1,2,4\}$ 3. Define Complemented Lattice with example. 01 .	02 04				
	(b)	Define Tautology and Contradiction with example. Prove that $p \rightarrow (p V q)$ is tautology without constructing truth table.	07				
Q.2	(a)1.	 (a)1. Define Group. Check Whether <i, ×=""> forms a group or not where I is the of Integers and × is multiplication operation.</i,> 2. Define Sum-Of Product canonical form. Write Boolean Expression x₁ * in an equivalent sum-of-product canonical form in three variables x₁, x₂ = x₃. 					
	(b)	For an integer prove that the following statements are equivalent: p: x is divisible by 6. q: x is divisible by 2 and 3. r: x is an even number and x is divisible by 3. OR	07				
	(b)	Define equivalence relation. Let Z be the set of integers and R be the relation called Congruence modulo 5" defined by $R = \{ \langle x, y \rangle x \in Z^{\wedge} y \in Z^{\wedge} (x - y) \text{ is divisible by 5} \}$ Show that R is an equivalence relation. Determine the equivalence classes generated by the elements of Z.	07				
Q.3	(a)	Define Cyclic group. Write down the properties of cyclic group. Show that	07				
	(b)	$\langle Z_6, +_6 \rangle$ is a cyclic group of order 6 and also find its generators. Find a minimal sum-of-product form using K-map (i) α (x, y, z) = xyz + xyz' + x'yz' + x'y'z (ii) α (x, y, z) = xyz + xyz' + xy'z + x'yz + x'y'z OR	07				
Q.3	(a)	Define Sub Boolean Algebra. Find all sub-algebras of Boolean algebra $\langle S_{30}, *, \oplus, \cdot, 0, 1 \rangle$. Write proper steps.	07				
	(b)1.	Define Join Irreducible element, Meet irreducible element, Atom and Anti atom.	04				
		2. Explain Stone's Representation theorem with proper example. 03					

Q.4 (a)1. Define weakly connected, unilaterally connected and strongly connected graphs.

2. Define weak, unilateral and strong components. Find the strong, unilateral and weak components for the following digraph. 04



(b) Draw di-graph and find in-degree and out-degree of each vertex from the given adjacency matrix. Using adjacency matrix, find total numbers of path of length 1 and 2 between each vertex.

A =	1	1	1
	1	1	1
	1	1	1
	C		J

OR

Q.4	(a)	(a) Define Sub-group. Find the subgroups of $\langle Z_{10}, +_{10} \rangle$				
	(b) Define "Lattice as an Algebraic System", "Complete Lattice" and					
		"Distributive Lattice.				
		Let the sets S0, S1,, S7 be given by				
	$S0 = \{a, b, c, d, e, f\}, S1 = \{a, b, c, d, e\}, S2 = \{a, b, c, e, f\}, S3 = \{a, e\}, S4 = \{a, b, c\}, S5 = \{a, b\}, S6 = \{a, c\},$					
		Draw the diagram of $<$ L, \subseteq >,				
		where $L = \{S0, S1, S2, \dots, S7\}$				
	Q.5	(a)	1. Explain path and circuit with example. 04	Ļ		
		2. Test the validity of the logical consequence given below:				
		All birds can fly.				
		A sparrow is a bird.				
		Therefore, a sparrow can fly. 03				
	(b)	Find minimal SOP using Quine Mc-cluskey method	07			
		$F(a,b,c,d) = \Sigma (0,1,2,5,6,7,8,9,10,14)$				
		OR				
Q.5	(a)1.	Let R be a relation on N such that aRb if and only if a b (a divides b)				
		in N. Check whether R is an equivalence relation or not?				

2. Let R and S be two relations on a set of positive integers I, $R = \{<x, 3x > /x \in I\}$ $S = \{<x, 4x > /x \in I\}$ Then find R 0 R and R 0 S 0 R. 02

3. Let $S = \{2,4,5,10,15,20\}$ and the relation \leq is the divisibility relation. Draw the Hasse diagram of $\langle S, \leq \rangle$. **02**

07

(b) Define Group Homomorphism. Define isomorphic groups. Prove that groups $\langle Z_6, +_6 \rangle$ is isomorphic to $\langle Z_7^*, *_7 \rangle$, where $Z_7^* = Z_7 - [0]$
