GUJARAT TECHNOLOGICAL UNIVERSITY MCA - SEMESTER-I • EXAMINATION – SUMMER • 2015

Subject Code: 610003 Date: 07-05-201			
Su	ibject	t Name: Discrete Mathematics for Computer Science	
Ti	me: 1	10:30 am - 01:00 pm Total Marks: 70	
Instructions: 1. Attempt all questions. 2. Make suitable assumptions wherever necessary. 3. Figures to the right indicate full marks.			
Q.1	(a)	(i)Test the validity of the following logical consequence. If Chris studies, then he will pass the class test. If Chris does not play cards, then he will study. Chris did not pass in the class test. Therefore, Chris played cards. (ii) Give direct proof to show that if x is an even integer then $x^2 + x$ is also an	03
	(b)	even integer. Explain Universal quantification, Universal quantifier, Existential quantification and Existential quantifier.	04 07
Q.2	(a)	Draw Hasse diagram of following lattices (i)(S ₃₆ ,D) (ii)(S ₄₅ D)	07
	(b)	Let (L,\leq) be a lattice and a, b $\in L$ then prove that $a\leq b \Leftrightarrow a*b = a \Leftrightarrow a \oplus b = b$ OR	07
	(b)	State and prove absorption law for lattice $\langle L, \leq \rangle$.	07
Q.3	(a)	Find a minimal sum-of-product using K-map (i) α (x, y, z) = xyz + xyz' + x'yz' + x'y'z (ii) α (x, y, z) = xyz + xyz' + xy'z + x'yz + x'y'z.	07
	(b)	Find all Sub Boolean algebras of Boolean algebra < S_{30} , Λ , V , ' , 0 , 1 >. OR	07
Q.3	(a) (b)	 Define: i) Join irreducible elements. ii) Atoms of a Boolean algebra. Determine Join-irreducible elements and atoms of (S₂₁₀, D) Let X = {a b c} then show that < P(X) or the X > is complemented lattice. 	07
0.4	(0)	Let $X = \{a, b, c\}$ then show that $< T(X), (a, b), (a, b)$ is complemented fattice.	07
Q.4	(a) (b)	Find all left and right cosets of $H=\{p_1,p_5,p_6\}$ in (S_3,D) . Where (S_3,D) is a symmetric group. Show that cyclic group is abelian group but converse is not true.	07
	(0)	OR	07
Q.4	(a)	Define cyclic group and subgroup. Show that $(\mathbb{Z}^*_{11}, \mathbf{x}_{11})$ is cyclic group. Find its all generators. Also find its all subgroups.	07
	(b)	Define Group Isomorphism. Show that $(Z_6,+_6)$ is isomorphic to (Z_7^*,\times_7)	07
Q.5	(a)	Obtain binary tree corresponding to following tree. (v0(v1(v2)(v3)(v4))(v5(v6)(v7)(v8)(v9))(v10(v11)(v12)))	07



OR

- Q.5 (a) Define complete binary tree. Show through two examples with nt = 7 and nt = 8 07 of complete binary trees that the total number of edges is given by 2(nt 1), where nt is the number of terminal nodes.
 - (b) Define: Node Base. Find all node bases for the following graph

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