

GUJARAT TECHNOLOGICAL UNIVERSITY**M.E Sem-I Examination January 2010****Subject code: 710422****Subject Name: Digital Signal Processing and Application****Date: 27/ 01 / 2010****Time: 12:00 - 2:30pm****Total Marks: 60****Instructions:**

1. Attempt all questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.

Q.1 (a) For each of the following systems, determine whether system is stable, causal, linear and time-invariant or not. **06**

(i) $y[n] = g[n]x[n]$ (ii) $y[n] = ax[n] + b$

(b) (i) Find the linear convolution of two sequences given by **02**

$x(n) = b^n u(n)$ for all n & $h(n) = a^n u(n)$ for all n

(ii) How can you find step response of a system if impulse response is known? Determine the step response of a linear-time-invariant system whose unit-impulse response is given by $h(n) = a^n u(-n)$, $0 < a < 1$ **04**

Q.2 (a) State sampling theorem. What is aliasing effect? **06**

A digital communication link carries binary coded words representing samples of an input signal $X_a(t) = 3\cos 600\pi t + 2\cos 800\pi t$. The link is operated at 10,000 bits/sec and each input sample is quantized into 1024 different voltage levels.

(i) What is sampling frequency and folding frequency?

(ii) What is Nyquist rate for the signal $X_a(t)$?

(iii) What are the frequencies in resulting discrete time signal?

(b) What is multirate signal processing? Explain application of Decimation and Interpolation to A/D and D/A conversion. **06**

OR

(b) (i) For difference equation $y(n) - 3y(n-1) - 4y(n-2) = x(n) + 2x(n-1)$ find frequency response $H(e^{j\omega})$ and impulse response $h(n)$ **03**

(ii) State properties of Region Of Convergence for z-transform **03**

Q.3 (a) Explain Decimation-in-time algorithm to calculate 8-point DFT **06**

(b) A causal LTI system has impulse response $h(n)$, for which the z-transform is $H(z) = (1+z^{-1}) / [(1-0.5z^{-1})(1+0.25z^{-1})]$ **06**

(i) What is the region of convergence of $H(z)$?

(ii) Is the system stable?

(iii) Find the z-transform $X(z)$ of an input $x[n]$ that will produce the output $y[n] = -(1/3)(-1/4)^n u[n] - (4/3)(2)^n u[-n-1]$

(iv) Find the impulse response $h[n]$ of the system.

OR

Q.3 (a) How to obtain linear convolution from circular convolution? Perform the circular convolution of $x[n] = \{1, 1, 2, 1\}$ and $h[n] = \{1, 2, 3, 4\}$ using DFT and IDFT method. **06**

(b) Distinguish between DFT and DTFT. List out the properties of DFT and explain circular shift of a sequence property of DFT. **06**

- Q.4 (a)** Design a low pass discrete time filter by applying bilinear transformation method to an appropriate Butterworth continuous time filter for the following specification. **08**
- (i) Passband magnitude is constant within 3 db for frequencies below 0.2π i.e $0 \leq \omega \leq 0.2\pi$
- (ii) Stopband attenuation is greater than 25 db for frequencies between 0.45π and π i.e $0.45\pi \leq \omega \leq \pi$. Consider T is equal to unity.
- (b)** Compare FIR and IIR digital filters **04**
- OR**
- Q.4 (a)** Give direct form I and direct form II structure of second order system realization. **04**
- (b)** What is Gibbs phenomenon? Design an FIR lowpass filter using Kaiser window filter design method satisfying the specifications $w_p=0.4\pi, w_s=0.6\pi, \delta_p=0.01, \delta_s=0.001$. **08**
- Q.5 (a)** Compare the fixed point and floating point arithmetic for DSP Processors. **04**
- (b)** Explain pipeline concepts in DSP. **04**
- (c)** List various application areas of DSP processors and describe application of DSP to speech processing. **04**
- OR**
- Q.5 (a)** Explain finite word length effects in FIR digital filters. **06**
- (b)** Describe Harvard Architecture in detail. **06**
