

**GUJARAT TECHNOLOGICAL UNIVERSITY**

M.E Sem-I Remedial Examination January/ February 2011

**Subject code: 712103****Subject Name: Fluid Mechanics and Gas Dynamics****Date: 02 /02 /2011****Time: 02.30 pm – 05.00 pm****Total Marks: 60****Instructions:**

1. Attempt all questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.
4. Use of gas tables is permitted.

**Q.1 (a)** Explain clearly velocity potential  $\phi$  and stream function  $\Psi$  and hence prove Cauchy - Riemann's equation in Cartesian co-ordinates? **06**

**(b)** Explain what do you understand by doublets? Show that the combine flow field of a uniform flow & a doublet gives the flow around the cylinder, Hence analyze the flow? **06**

**Q.2 (a)** Derive Euler's momentum equations in Cartesian coordinates system? **06**

**(b)** What is velocity of sound? From fundamental equation show that velocity of sound is given by  $a^2 = (\partial P / \partial \rho)_s$ . Hence obtain the expression of the velocity of sound in perfect gas & explain the effect of molecular weight on it? **06**

**OR**

**(b)** Derive continuity equation in cylindrical polar co-ordinates for a two dimensional fluid flow with usual notations. **06**

**Q.3 (a)** The power developed by hydraulic machine is found to depend on the head  $h$ , flow rate  $Q$ , density  $\sigma$ , speed  $N$ , runner diameter  $D$ , and acceleration due to gravity,  $g$ . Obtain suitable dimensionless parameter to correlate experimental results. You can adopt MLT set of dimensions. **06**

**(b)** Define stagnation temperature and critical temperature of a gas. Also derive the **06**

$$\text{equation } \frac{T^*}{T} = \left( \frac{2}{\gamma + 1} \right)$$

**OR**

**Q.3 (a)** Define Static and Stagnation enthalpies. Also prove that **06**

$$h_0 = h \left[ 1 + \left( \frac{\gamma - 1}{2} \right) M^2 \right]$$

**(b)** discuss the type of nozzles required for subsonic and supersonic flows **06**

$$\frac{dC}{C} = \left( \frac{1}{M^2 - 1} \right) \frac{dA}{A}$$

**Q.4 (a)** Explain Stream function for two dimensional fluid flow and give its properties. **06**

**(b)** Define the following terms for an aerofoil with figure: **06**

(1) Drag force (2) Chord length (3) Angle of attack (4) Span

**OR**

**Q.4 (a)** What is similitude and model testing? Define conditions for similarity between models and prototype with different similarity? Express types of model studies in brief? **06**

**(b)** Explain the difference between Source flow and Sink flow with figures. **06**

**Q.5 (a)** Using fundamental equation obtain the Rankine – Hugonout equation for a normal shock? Hence show that a normal shock can not compress the gas to a density more than six times the density on upstream side? Also show that product of upstream and downstream velocity is equal to a square of critical velocity of flow? **06**

**(b)** For a flow in a constant area duct in which friction is predominant & heat transfer negligible ,discuss **06**  
 a) Duct length limitation  
 b) Chocking due to friction, considering initial velocity as subsonic as well as supersonic.

**OR**

**Q.5 (a)** Derive the following equation for maximum heat transfer ( $Q_{max}$ ) for Rayleigh flow with usual notations. **06**

$$Q_{max} = C_p T_1 \cdot \frac{(1 - M^2)^2}{2(1 + \gamma)M^2}$$

**(b)** From fundamental equation prove that ,for the flow in constant area duct with heat transfer **06**

a)  $T_1/T_2 = (M_1/M_2)^2 (1 + \gamma M_2^2 / 1 + \gamma M_1^2)^2$

b)  $C_1/C_2 = \rho_2 / \rho_1 (M_1/M_2)^2 (1 + \gamma M_2^2 / 1 + \gamma M_1^2)$

c)  $S_2 - S_1 / R = \ln M_2/M_1 (M_2/M_1) (1 + \gamma M_1^2 / 1 + \gamma M_2^2)^{\gamma+1/(\gamma-1)}$

\*\*\*\*\*