

GUJARAT TECHNOLOGICAL UNIVERSITY

ME Semester –II Examination Dec. - 2011

Subject code: 1710404

Date: 16/12/2011

Subject Name: Image Processing

Time: 02.30 pm – 05.00 pm

Total Marks: 70

Instructions:

1. Attempt all questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.

Q.1 (a) The probability distribution of an 8-level image is specified under two contrast conditions by two histograms A and B as given below. **07**

Histogram A:

$$Pr(0)=0, Pr(1)=Pr(2)=0.1, Pr(3)=0.3, Pr(4)=Pr(5)=0, Pr(6)=0.4, Pr(7)=0.1$$

Histogram B:

$$Pz(0)=0, Pz(1)=0.1, Pz(2)=0.2, Pz(3)=0.4, Pz(4)=0.2, Pz(5)=0.1, Pz(6)=Pz(7)=0$$

Find the transformation between r and z

(b) Consider the image segment shown in below figure **07**

(i) Let $V=\{0,1\}$ and compute the lengths of the shortest 4-,8- and m-path between p and q

(ii) Repeat for $V=\{1,2\}$

| | | | |
|-------|---|---|-------|
| 3 | 1 | 2 | 1 (q) |
| 2 | 2 | 0 | 2 |
| 1 | 2 | 1 | 1 |
| 1 (p) | 0 | 1 | 2 |

Q.2 (a) Prove that for Laplacian Operation using $\nabla^2 f = \frac{\partial^2 f}{\partial x^2} + \frac{\partial^2 f}{\partial y^2}$ is isotropic **07**

for equations shown below relating coordinates after axis rotation by an angle θ

$$x = x' \cos \theta - y' \sin \theta$$

$$y = x' \sin \theta + y' \cos \theta$$

Where (x, y) are the unrotated and (x', y') are the rotated coordinates

(b) An image has the gray level PDF $Pr(r)$ shown in figure (1). It is desired to transform the gray levels of his images so that they will have the specified $Pz(z)$ shown. Assume continuous quantities and find the transformation in terms of r and z that will accomplish this. **07**

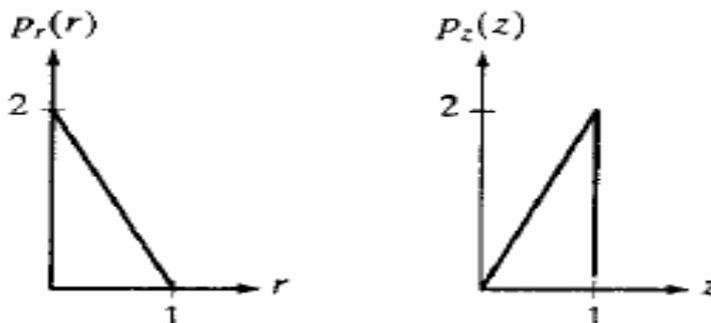


Figure 1

OR

(b) Explain Wiener filtering for removal of blur in image. **07**

Q.3 (a) Explain homomorphic filtering in detail. **07**

(b) Prove that $\nabla^2 f(x, y) \Leftrightarrow -(u^2 + v^2)F(u, v)$ **07**

OR

Q.3 (a) Define a model of Image restoration. Also explain the different noise Probability Density functions. **07**

(b) Explain the following terms: (1) JPEG 2000 (2) MPEG Standard. **07**

Q.4 (a) Explain the Hit or Miss transformation. **07**

(b) Explain the region filling and boundary extraction morphological algorithm. **07**

OR

Q.4 (a) (i) Show that the definition of dilation **07**

$$A \oplus B = \{w \in Z^2 \mid w = a + b, \text{ for some } a \in A \text{ and } b \in B\}$$

is equivalent to

$$A \oplus B = \bigcup_{b \in B} (A)_b$$

(ii) Show that another definition of dilation

$$A \oplus B = \{w \in Z^2 \mid (\hat{B})_w \cap A \neq \Phi\}$$

is also equivalent to

$$A \oplus B = \bigcup_{b \in B} (A)_b$$

Q.4 (b) What do you mean by Color model? List the application of each color model. Explain any one color model in brief. **07**

Q.5 (a) What is the advantage of using Sobel operator? Explain the process of edge detection using gradient operators. **07**

(b) Explain the concept of Laplacian and LoG for edge detection and comment on comparison of both the operators. **07**

OR

Q.5 (a) Explain the concept of edge linking using Hough transform. **07**

(b) Explain the concept of thresholding in image segmentation and two methods of thresholding in brief. **07**
