

Seat No.: \_\_\_\_\_

Enrolment No. \_\_\_\_\_

**GUJARAT TECHNOLOGICAL UNIVERSITY**  
**ME - SEMESTER– I (OLD course)• EXAMINATION – SUMMER 2015**

**Subject Code:** 714101

**Date:** 11/05/2015

**Subject Name:** Mathematical Methods in Signal Processing

**Time:** 10:30 am to 1:00 pm

**Total Marks:** 70

**Instructions:**

1. Attempt all questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.

**Que 1) a)** Compute transpose, inverse and rank of the matrix A , [7]

$$A = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 4 & 6 \\ 3 & 6 & 9 \end{bmatrix}$$

- b)**
- i) Explain why the set of real numbers is both open and closed. [7]
  - ii) Show that the boundary of a set S is a closed set.

**Que 2) a)** Explain about binary hypothesis testing. [7]

- b)** Explain any one method of signal detection and estimation with suitable example. [7]

**OR**

- b)** Let  $(X, d)$  be a metric space show that  $d_m(x, y) = \min(1, d(x, y))$  is a metric on X. [7]

**Que 3) a)** Obtain Z- transform of unit step and unit impulse. [7]

- b)** What is Bayes approach? List out applications of the approach in signal processing. [7]

**OR**

**Que 3) a)** i) A linear operator  $A: X \rightarrow Y$  is bounded if and only if it is continuous. Justify the statement. [7]

- ii) Consider a data sequence  $\{x|t|\}$ , the correlation matrix R is

$\begin{bmatrix} .5 & .3 \\ .3 & .5 \end{bmatrix}$  and the cross correlation vector  $p$  with a desired signal is  $\begin{bmatrix} .2 \\ .5 \end{bmatrix}$ . Determine the optimal weight vector.

- b) A Grammian matrix  $R$  is always positive semi define. It is positive define if and only if the vectors  $p_1, p_2, p_3, \dots, p_m$  are linearly independent. [7]

**Que 4) a)** Explain Modulation Theorem and Parseval's Theorem. [7]

- b) Explain LMS algorithm with application. [7]

**OR**

**Que 4) a)** Find eigen values and corresponding eigen vector of the matrix  $A$  [7]

$$A = \begin{bmatrix} 8 & -6 & 2 \\ -6 & 7 & -4 \\ 2 & -4 & 3 \end{bmatrix}$$

- b) [7]

For matrix  $T$  in block triangular form  $T = \begin{bmatrix} T_{11} & T_{12} \\ 0 & T_{22} \end{bmatrix}$

show that  $\lambda(T) = \lambda(T_{11}) \cup \lambda(T_{22})$

**Que 5) a)** Explain Linearity and scaling property of Fourier Transform. [7]

- b) Let  $A: H \rightarrow H$  be a bounded linear operator on a Hilbertspace  $H$ . Show that: [7]

i) The adjoint operator  $A^*$  is linear.

ii) The adjoint operator  $A^*$  is bounded

iii)  $\|A\| = \|A^*\|$ .

**OR**

**Que 5) a)**

Let  $A = \begin{bmatrix} 3 & 2 \\ 4 & -1 \end{bmatrix}$ , using Cayley-Hamilton calculate  $A^9$ . [7]

**b)** Determine the Jordan form of A. [7]

$$A = \begin{bmatrix} 2 & 1 & 1 \\ 0 & 1 & 0 \\ 1 & 1 & 2 \end{bmatrix}$$