

**GUJARAT TECHNOLOGICAL UNIVERSITY****M. E. - SEMESTER – I • EXAMINATION – WINTER 2012****Subject code: 711901N****Date: 08-01-2013****Subject Name: Modeling, Analysis & Simulation****Time: 02.30 pm – 05.00 pm****Total Marks: 70****Instructions:**

1. Attempt all questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.

- Q.1** (a) Define mathematical model. Why it is said that a model is an idealized representation of reality? How mathematical models are classified & how do they differ in their predicting capability. **07**
- (b) How would you define a process of vehicles on highway using discrete and continuous distributions? **07**

- Q.2** (a) It is found that the percentage of left vehicles from eastbound approach is 20% and average hourly volume of eastbound is 2000vph. The cycle length for this intersection is 90 seconds. Estimate the probability that no more than 4 left turn vehicles will come in a cycle. **07**
- (b) Why do we need random numbers? Can we generate truly random numbers or random fractions? **07**

**OR**

- (b) What is Gamma Family distribution? List them along with their mean and variance. Plot the Erlang distribution. **07**

- Q.3** (a) Find the variance of Poisson distribution from the basic property of moment of discrete distributions. What is its M.G.F.? **07**
- (b) What is Monte-Carlo Simulation? Use Monte-Carlo method to find the value of  $\pi$ . **07**

**OR**

- Q.3** (a) What are the advantages of Simulation? Explain in detail “various steps used in a simulation study”. **07**
- (b) Describe the importance of random numbers in simulation. **07**

- Q.4** (a) Vehicles arrivals at the main gate of park are assumed Poisson distribution with an average arrival rate of 1 vehicle every 5 minutes. What is the probability of the following: **07**
- (i) Exactly 2 vehicles arrive in a 15 minute interval?
- (ii) Less than 2 vehicles arrive in a 15 minute interval?
- (iii) More than 2 vehicles arrive in a 15 minute interval?
- (b) Based on survey, 25% commuters choose transit for their daily trip. There are 5 commuters being randomly selected from an organization. Estimate the probability that 1 person among 5 will choose transit for travel. **07**

**OR**

- Q.4** (a) What are stochastic processes and/ or stochastic events? Give some examples & show whether these can be converted into probabilistic processes? **07**
- Q.4** (b) “Traffic flow is one of the most difficult processes to be modeled in space-and-time”. Why? **07**

**Q.5** (a) Explain the application areas of queuing and explain different terminologies used in queuing system. **07**

(b) What are auxiliary functions in study of probability density functions? **07**

**OR**

**Q.5** (a) List and explain the conditions when simulations become essential and desirable. **07**

(b) What do you understand by Pseudo-random numbers generated by Multiplicative Congruent Techniques (MCT)? **07**

Explain:  $A-B=k*m$

$A=B \pmod{m}$

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