Enrolment No.

# GUJARAT TECHNOLOGICAL UNIVERSITY M. E. - SEMESTER - I • EXAMINATION - WINTER • 2013

Subject code: 712103N Subject Name: Fluid Mechanics & Gas Dynamics Time: 10.30 am – 01.00 pm

Date: 03-01-2014

**Total Marks: 70** 

# **Instructions:**

- 1. Attempt all questions.
- 2. Make suitable assumptions wherever necessary.
- 3. Figures to the right indicate full marks.
- 4. Use of Gas Table is permitted.
- 5. Usual notations are used.

Q.1 (a) Derive the following equation and draw the shape of nozzle and diffuser for 07

subsonic, sonic and supersonic flow. 
$$\frac{dA}{A} = \frac{\partial p}{\rho c^2} \left(1 - \frac{c^2}{a^2}\right)$$

- (b) Air ( $\gamma$ =1.4, R=287.43 J/kg K) enters a straight axisymetric duct at 300 K, 3.45 07 bar and 150 m/s and leaves it at 277 K, 2.058 bar and 260 m/s. The area of cross section at entry is 500 cm<sup>2</sup>. Assuming adiabatic flow determine (i) stagnation temperature (ii) maximum velocity (iii) mass flow rate (iv) area of cross section at exit.
- Define geometric, kinematic and dynamic similarities. Explain how the Q.2 07 (a) condition of dynamic similarity of a hydraulic model is satisfied in actual practice.
  - (b) Derive equivalent Bernoulli's equation for isentropic compressible flow.

$$\frac{\gamma}{\gamma - 1} \frac{P_0}{\rho_0} \left( \frac{P}{P_0} \right)^{\frac{\gamma - 1}{\gamma}} + \frac{1}{2}c^2 = \frac{\gamma}{\gamma - 1} \frac{P_0}{\rho_0}$$

## OR

(b) The pressure drop  $\Delta P$  in pipe of diameter D and length L depends on the 07 density  $\rho$  and viscosity  $\mu$  of the fluid flowing, mean velocity V of flow and the average height of protuberance 't'. Show that the pressure drop can be

expressed in the form : 
$$\Delta P = \rho V^2 f\left(\frac{L}{D}, \frac{\mu}{VD\rho}, \frac{t}{D}\right)$$

- (a) Derive an equation describing a Fanno curve. Show three Fanno curves on the 0.3 07 T-s coordinates at three mass flow densities.
  - The friction factor for a 25 mm diameter 11.5 m long pipe is 0.004. The **(b)** 07 conditions of air at entry are p<sub>1</sub>=2.0 bar, T<sub>1</sub>=301 K, M<sub>1</sub>=0.25. Determine the mass flow rate, and pressure, temperature and Mach number at exit.

#### OR

- Determine  $\psi$  for a steady flow of 20 m/s down and to the right at 45 degree to Q.3 (a) 07 the y-axis.
  - (b) Explain doublets and vortices with necessary diagrams. 07
- Draw a Rayleigh line on T-s plane. Show the following on this line: (a) 07 **Q.4** (a) stagnation temperature lines for both subsonic and supersonic flows (b) maximum stagnation temperature point (c) constant static and stagnation pressure lines.

07

(b) The stagnation temperature of air in a combustion chamber is increased to 3.5 07 times its initial value. If the air at entry is at 5 bar, 105°C and a Mach number of 0.25. Determine (a) the Mach number, pressure and temperature at the exit, (b) stagnation pressure loss and (c) the heat supplied per kg of air.

#### OR

- Q.4 (a) Derive the momentum equation for compressible fluid flow under steady state 07 conditions
  - (b) Derive Kutta-Joukowski equation for lift of a cylinder.

- 07
- Q.5 (a) Using the equation of change in entropy across shock wave, prove that it is 07 impossible to have shock wave in subsonic flow.
  - (b) A Mach -2 aircraft engine employs a subsonic inlet diffuser of area ratio 3. A normal shock is formed just upstream of the diffuser inlet. The free stream conditions upstream of the diffuser are: p= 0.10 bar, T= 300 K. Determine (a) Mach number, pressure and temperature at the diffuser exit. (b) Diffuser efficiency including the shock. Assume isentropic flow in the diffuser downstream of the shock.

## OR

- Q.5 (a) What is an aerofoil? Define Drag and Lift co-efficient in reference of aerofoil. 07 Also explain the variation in the value of the coefficient of lift and the coefficient of drag of an aerofoil with angle of incidence.
  - (b) Explain the following: (i) Mach angle (ii) Mach cone (iii) Mach wave (iv) Zone
    07 of action (v) Zone of silence (v) stagnation Temperature (vi) critical velocity.

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